

On Algebra and Tachyons

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Abstract: Problem statement: After formulating the special theory of relativity in 1905, Albert Einstein politely remarked: “for velocities that are greater than light, deliberations become meaningless”. In 1962, Sudarshan and his co-researchers proposed a hypothesis that particles/objects whose rest mass is imaginary can travel by birth faster than light. After publication of Sudarshan’s research, many scholars began to probe into faster than light phenomena. In extended relativity, many properties of tachyons have been found. But still this micro second, the velocity of a tachyon with respect to us is unknown. In this research the researchers found the tachyon velocity. **Approach:** In this research, Einstein’s variation of mass with velocity equation was transformed into quadratic equation. We introduced a new hypothesis to find the roots of the quadratic equation. **Results:** By introducing a new hypothesis in tachyon algebra, the researchers found that the velocity of superluminal objects with respect to us is $v = c\sqrt{3}$ where c is the velocity of the light. **Conclusion/Recommendations:** But the road to tachyon is too long. Hereafter it is up to experimental physicists to establish the existence/generation of tachyons.

Key words: Einstein, special theory of relativity, superluminal hypothesis, superluminal phenomena, quadratic equations and new conjectures.

INTRODUCTION

Algebra is one of the most powerful tools to study other branches of mathematics. For example, the application of modern algebra enabled us to see that it is impossible to solve the classical problems of trisection of a general angle without using a protractor, squaring the circle, doubling the cube and to draw a regular septagon [2]. In this study, the researchers introduced a new conjecture on quadratic equations which dates 2000 B.C. and located tachyon velocity with respect to us.

Assuming Sudarshan’s tachyon hypothesis in Einstein’s variation of mass with velocity eqn. we get that [1-3] (1) where m is the moving mass of the tachyon, m_0 is the rest mass, $v > c$ and i is imaginary:

$$m^2(1-n) = i^2 \quad (1)$$

$$m^2(n-1) = -1$$

$$m^2(n-1) = 1 \quad (1a)$$

$$n-1 = 1/m^2 \quad (1b)$$

$$m^2 n = m^2 + 1 \quad (1c)$$

$$\text{Multiplying by } n, m^2 n^2 = m^2 n + n$$

Using 1c in RHS:

$$m^2 n^2 - n - m^2 - 1 = 0 \quad (2)$$

Equation 2 is quadratic in n .

According to the laws of quadratic eqns. if K and L are the roots:

$$K+L = -b/a \quad (3)$$

$$KL = c/a \quad (4)$$

Applying (3) and (4) in (2), $K+L = 1/m^2$, $KL = -(m^2+1)/m^2 = -1-1/m^2$:

$$\text{Adding } K+L + KL + 1 = 0$$

$$(K+1)(L+1) = 0 \quad (5)$$

From (5) we have:

$$K = -1 \tag{5a}$$

Squaring (1a):

$$m4n^2-2m4n+m4-1 = 0 \tag{6}$$

Equation 6 is also quadratic in n.

Assuming (3) and (4) in (6), $K+L = 2m4/m4 = 2$:

$$KL = m4-1/m4 = 1 -1/m4$$

$$\text{Adding } K+L+KL = 3-1/m4$$

Using (1b) in RHS:

$$K+L+KL = 2-n^2+2n \tag{7}$$

In both the quadratic Eq. 2 and 6 the roots K and L denote the velocity of one and the same tachyon. So, putting (5a) in (7) $n^2-3-2n = 0$:

$$(n+1)(n-3) = 0 \tag{8}$$

$$n = -1$$

$$n = 3 \tag{8b}$$

If we put $n = -1$ in (2) the equation becomes $4m^2 = 1$ and if we apply $n = -1$ in (6),

$$4m^2 = 1$$

$$2m^2 = 1 \tag{9a}$$

using (9a) in (1a) we get $m = 1/\sqrt{2}$. Applying (8b) in (5) we get (9). i.e., $4m^2 = 1$

So, $n = [3, -1]$ is the solution set. Since $n = v^2/c^2$, we get that:

$$v = c/\sqrt{3} \tag{10}$$

i.e., the velocity of a free tachyon w.r.to us is $c/\sqrt{3}$.

MAINTAINING METHODS

The researcher politely request the research community to attempt/apply this conjecture to the other fields of mathematical sciences.

RESULTS AND DISCUSSION

It was the Babylonians who gave the solution formula $x = -B \pm [B^2-4AC]^{1/2}$ for the quadratic Eq. 2 of

the general form $Ax^2+Bx+C = 0$. Quadratic equation is an interesting mathematical topic. The members of the British parliament had a nice debate on June 17, 1993 on this topic. Even Einstein's formula $E = mc^2$ is also a quadratic equation. We can not find the solution of the Eq. 2 and 6 by applying the classical formula. That's why the authors introduced and assumed the above hypothesis. Replacing $m = c/\sqrt{2}$ and $n = 3$ the Eq. 1, 2 and 6 satisfy. So, the above hypothesis is acceptable and agreeable.

CONCLUSION

It is well known that experimental verification is the supreme judge in physics. The result is consistent in theoretical physics, it is also consistent in experimental physics also. Albert Einstein requested the physicists to locate solutions for the burning problems of physics in the eastern spiritual philosophy. Thripura Rahasya is one of the most famous meta physics in Hinduism. The great sage Thathathreya reveals the existence of tachyons in this masterpiece. If tachyons are inconsistent, it is not easy to derive Eq. 8b. Here it is up to experimental physicists to locate or generate tachyons.

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